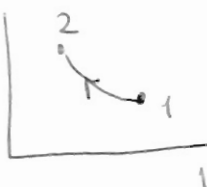


PHYSICS 2 - SUMMER 08 HOMEWORK 6

①

19.3 (a) $pV = \text{constant}$

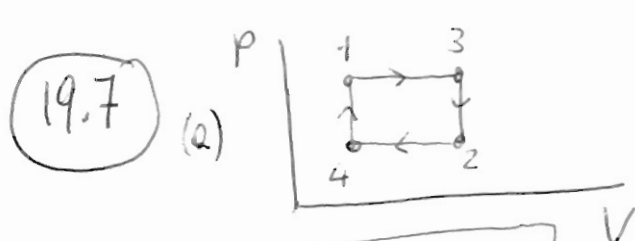


b) ~~isothermal~~ ~~work~~

$$W = nRT \log \frac{P_1}{P_2} \quad (\text{see example 19.1 on page 649})$$

$$P_1 V_1 = P_2 V_2 \quad P_2 = 3P_1$$

$$W = nRT \log \frac{1}{3} = -nRT \log 3 \quad W = -6540 \text{ J}$$



$$W = P_1(V_1 - V_2) - P_2(V_1 - V_2) \quad \boxed{W = (P_1 - P_2)(V_1 - V_2)}$$

(b) $\boxed{W = -(P_1 - P_2)(V_1 - V_2)}$

19.15 (a) Volume constant $\rightarrow W = 0$

(b) $pV = nRT$ since $V = \text{constant}$ and P doubles, T also doubles, i.e. $T_b = 2T_a$

(c) since $W = 0$, $\Delta U = Q = +400 \text{ J} \Rightarrow U_b = U_a + 400 \text{ J}$

19.16 (a) $a \rightarrow b$ greatest work on path 1
smallest work on path 3

(b) $\Delta U = Q - W$

$\Delta U > 0$ and path independent. $Q = \Delta U + W$
 $W > 0$ for all paths

$\Rightarrow Q$ greatest when W is greatest and $Q > 0$ (ie, heat is absorbed)

$$(19.24) \quad PV = nRT \Rightarrow P \Delta V = nR \Delta T \quad (\text{at constant } P) \quad (2)$$

$$\Rightarrow \Delta T = \frac{P \Delta V}{nR} > 0$$

$$Q = nC_p \Delta T \Rightarrow \text{heat absorbed } (Q > 0)$$

$$(19.30) \quad C_p = C_v + R \quad \text{and } \gamma = \frac{C_p}{C_v} \Rightarrow C_p = \gamma C_v$$

$$\gamma C_v = C_v + R \Rightarrow \boxed{C_v = \frac{R}{\gamma - 1}} \quad C_v = 65.5 \frac{\text{J}}{\text{mol K}}$$

$$\textcircled{C} \quad C_p = C_v + R = \frac{R}{\gamma - 1} + R = \frac{R + \gamma R - R}{\gamma - 1} \quad \boxed{C_p = \frac{\gamma}{\gamma - 1} R} \quad C_p = 73.8 \frac{\text{J}}{\text{mol K}}$$

$$(19.48) \quad W_{acb} = W_{a \rightarrow c} + W_{c \rightarrow b} + W_{b \rightarrow a} \quad (1)$$

$$W_{a \rightarrow c} = P_A (V_c - V_A) \quad \text{~~W}_{a \rightarrow c} = P_A (V_c - V_A)~~$$

$$W_{a \rightarrow c} = nR(T_c - T_a) = 3 \cdot 8.3145 \cdot (492 - 300) \text{ J} = \underline{4.789 \cdot 10^3 \text{ J}}$$

$$W_{c \rightarrow b} = Q - \Delta U = -\Delta U = -nC_v \Delta T = -n(C_p - R)(T_b - T_c)$$

$$W_{c \rightarrow b} = -3 \cdot (29.1 - 8.3145)(600 - 492) \text{ J} = \underline{-6.735 \cdot 10^3 \text{ J}}$$

$$W_{b \rightarrow a} = 0$$

$$\text{Adding all up according to eqn (1), } W_{acb} = \underline{-1.95 \cdot 10^3 \text{ J}}$$

$$(20.3) \quad (a) \quad e = \frac{\text{Work output}}{\text{heat input}} = \frac{3700}{16,100} = \underline{\underline{23\%}}$$

$$(b) \quad W = |Q_H| - |Q_C| \Rightarrow |Q_C| = |Q_H| - W = 16,100 - 3700 = \underline{\underline{12,400 \text{ J}}}$$

$$(c) \quad Q_H = mL_c \quad \text{where } L_c = \text{latent heat of combustion}$$

$$m = \frac{Q_H}{L_c} = \frac{16,100 \text{ J}}{4.6 \cdot 10^4 \text{ J/g}} = \underline{\underline{0.350 \text{ g}}}$$

(d) $W = 3700 \text{ J/cycle}$, $60 \text{ cycles/sec} \Rightarrow \text{Power} = 60 \times 3700 =$ (3)
 $\text{Power} = 222 \text{ } \cancel{10^3} \text{ } 10^3 \text{ W}$

$222 \text{ } \cancel{10^3} \text{ } 10^3 \text{ W} = 222 \text{ } 10^3 \text{ W} \frac{1 \text{ hp}}{746 \text{ W}} = \underline{298 \text{ hp}}$

(20.6) $e = 1 - \frac{1}{r^{\gamma-1}} \quad e = 1 - \frac{|Q_c|}{|Q_H|}$

(a) $e = 1 - \frac{1}{9.50^{0.40}} = \underline{59\%}$

(b) $|Q_c| = |Q_H| (1 - e) = \underline{4060 \text{ J}}$

(20.14) (a) $Q_c = -Q_H \frac{T_c}{T_H} = -6.45 \text{ } 10^3 \text{ J} \frac{300}{520} = \underline{-3.7 \text{ } 10^3 \text{ J}}$

(b) $|W| = |Q_H| - |Q_c| = \underline{2.73 \text{ } 10^3 \text{ J}}$

(c) $e = \frac{W}{Q_H} = \underline{42.3\%}$

(20.26) $Q_{\text{system}} = 0 \quad Q = mc \Delta T$

Example 20.6 shows $\Delta S = mc \log \frac{T_2}{T_1}$ for temp change

(a) Heat transfer $100^\circ\text{C} \rightarrow 30^\circ\text{C}$ is irreversible

(b) $270 \text{ kg } c (T_2 - 30^\circ\text{C}) + 5 \text{ kg } c (T_2 - 100^\circ\text{C}) = 0$ gives $\underline{T_2 = 31.27^\circ\text{C}}$

(c) $\Delta S = mc \log \frac{T_2}{T_1}$ gives $c = 4190 \text{ J/kgK}$

$\Delta S = 270 \text{ kg } c \log \frac{304.42}{303.15} + 5 \text{ kg } c \log \frac{304.42}{373.15}$

$\Delta S = \underline{+470 \text{ J/K}}$