

when

$$\theta_t = 90^\circ = \frac{\pi}{2}$$

$$n_1 \sin \theta_i = n_2$$

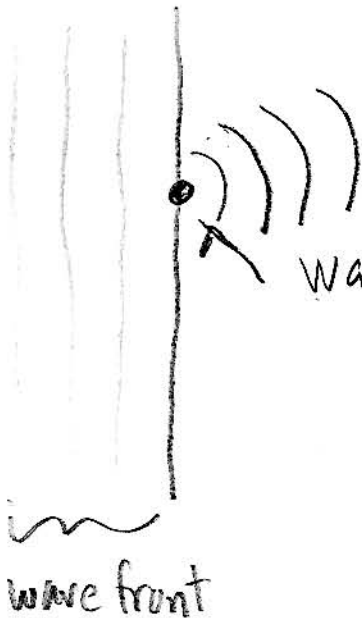
$$\sin \theta_i = \frac{n_2}{n_1} < 1$$

when $\theta_i > \sin^{-1}\left(\frac{n_2}{n_1}\right)$,

"total internal reflection"

next time you swim, look up from underwater.

Fermat's Principle



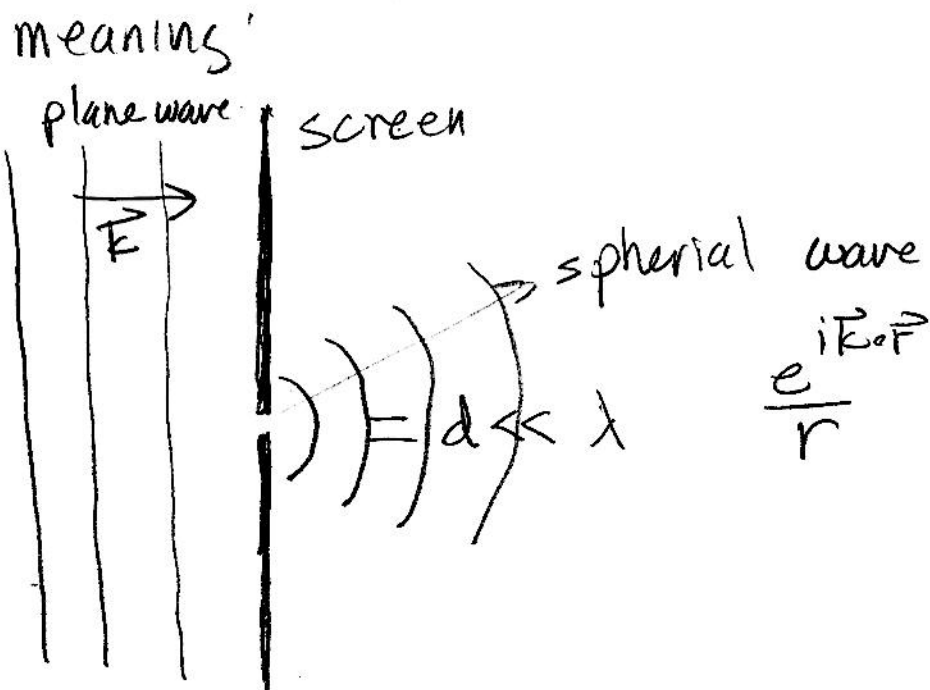
wave front: like a source of a new spherical wave

$$e^{i\vec{k} \cdot \vec{r}}$$

$$\frac{e}{r}$$

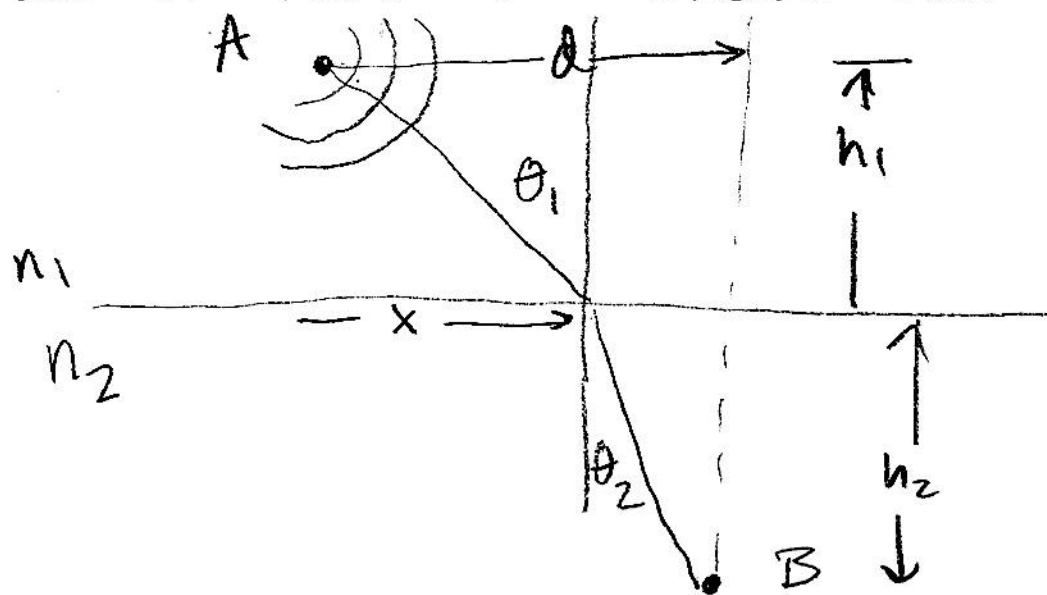
$$|\vec{k}| = \frac{2\pi}{\lambda}$$

$$\frac{1}{r^2} \text{ power} \propto \frac{1}{r^2}$$



integrate to
over
wavefront
propagate.

another view of Snell's Law.



Snell's law: $n_1 \sin \theta_1 = n_2 \sin \theta_2$
 is the path that minimizes the time
 it takes to go from point A to point B

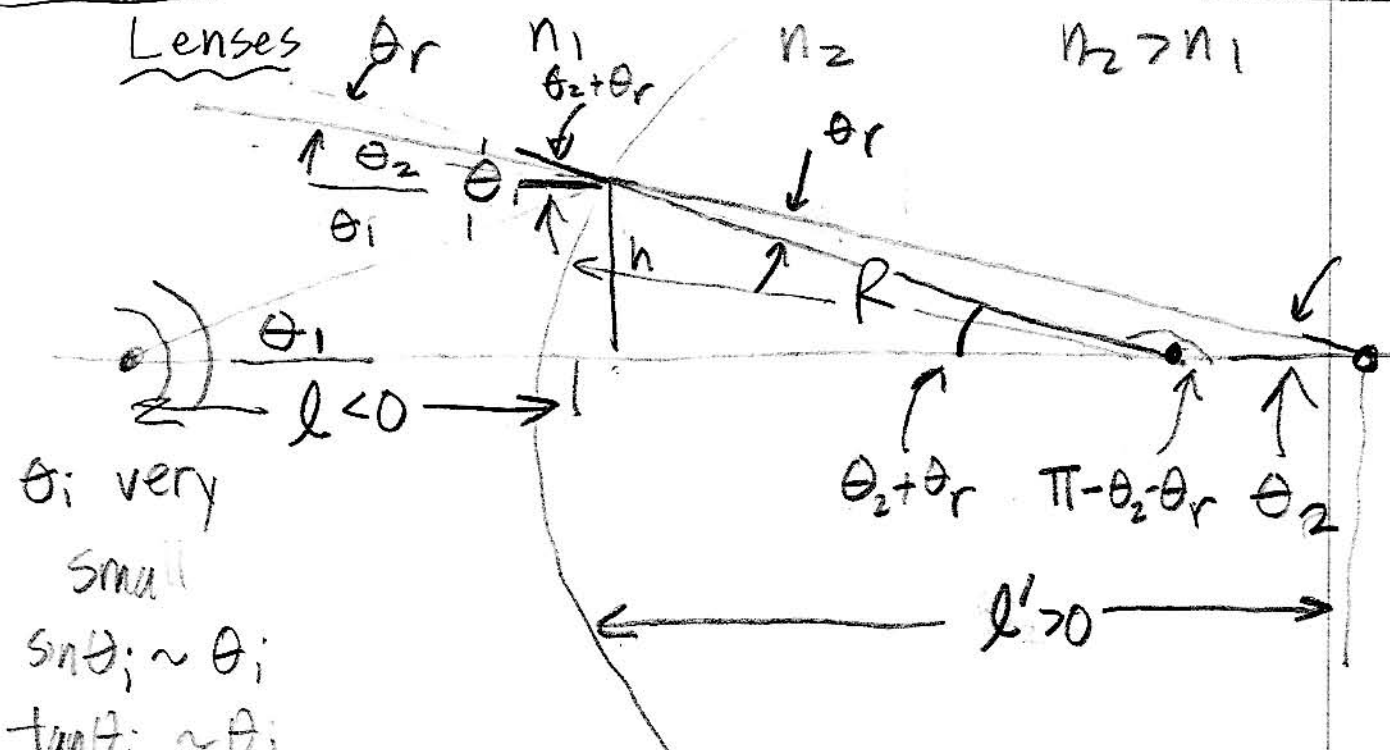
$$T_{BA} = \frac{\sqrt{h_1^2 + x^2}}{c/n_1} + \frac{\sqrt{h_2^2 + (d-x)^2}}{c/n_2}$$

$$\frac{dT}{dx} = \frac{n_1}{c} \frac{x}{\sqrt{h_1^2 + x^2}} - \frac{n_2}{c} \frac{x}{\sqrt{h_2^2 + (d-x)^2}}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

This is an illustration of "Fermat's Principle," that....

$\int_{A, \text{ path}}^B n(x) dx$ is an extremum for actual path



θ_i very small
 $\sin \theta_i \sim \theta_i$
 $\tan \theta_i \sim \theta_i$
 $\cos \theta_i \sim 1$

$$\theta_i' = \theta_1 + \theta_2 + \theta_r$$

$$\theta_1 \approx -\frac{h}{l} \quad \theta_2 \approx \frac{h}{l'}$$

$$n_1 \theta_i = n_2 \theta_r \quad (\text{small angle snell}).$$

$$\theta_2 + \theta_r = \frac{h}{R}$$

$$\theta_r = \frac{h}{R} - \frac{h}{l'}$$

$$\theta_i = \left(\frac{n_2}{n_1}\right) \theta_r = \left(\frac{n_2}{n_1}\right) h \left(\frac{1}{R} - \frac{1}{l'}\right)$$

$$n_2 \theta_i = \theta_1 + \theta_2 + \theta_r$$

$$\frac{n_2}{n_1} h \left(\frac{1}{R} - \frac{1}{l'}\right) = -\frac{h}{l} + \frac{h}{l'} + \frac{h}{R} - \frac{h}{l'}$$

$$n_2 \left(\frac{1}{R} - \frac{1}{l'}\right) = n_1 \left(\frac{1}{R} - \frac{1}{l}\right)$$

$$\frac{n_2}{l'} - \frac{n_1}{l} = \frac{(n_2 - n_1)}{R}$$

independent
of l !

for $n_2 < n_1$, the light penetrating the n_2 region diverges