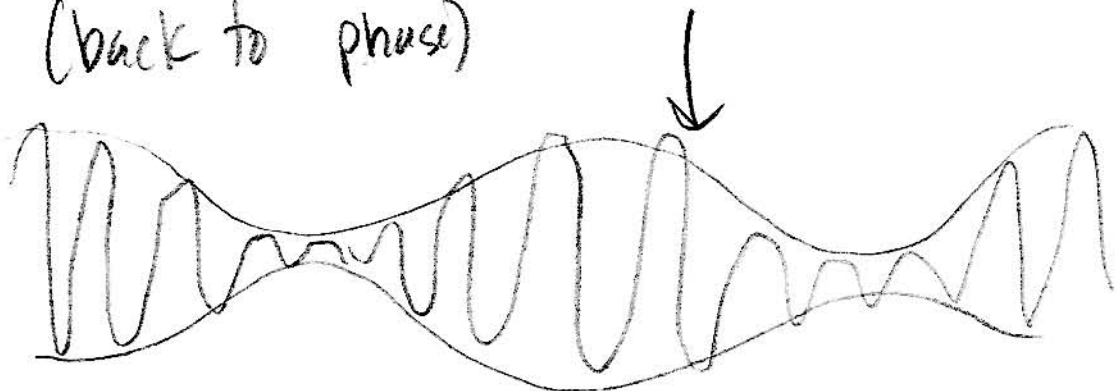
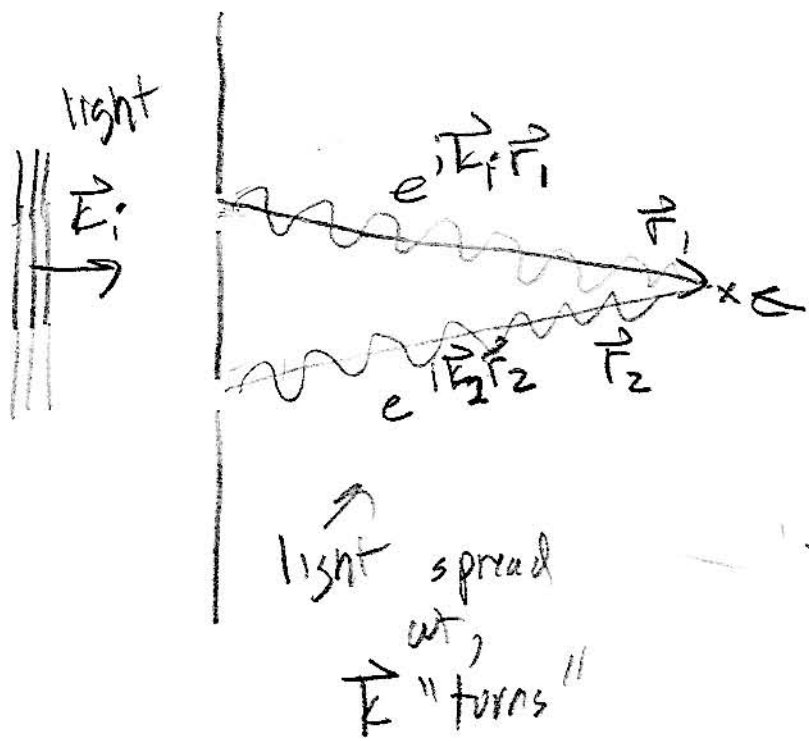


(back to phase)



Interference:



$$|\vec{r}_1| = |\vec{r}_2|$$

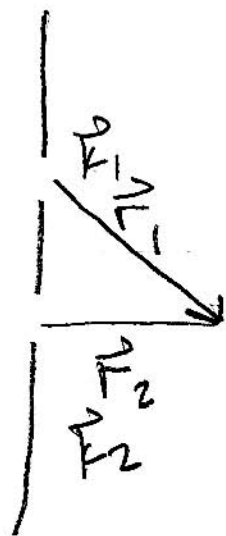
$$\vec{k}_1 \cdot \vec{r}_1 = \vec{k}_2 \cdot \vec{r}_2$$

"in phase"

$$e^{i\vec{k}_1 \cdot \vec{r}_1} + e^{i\vec{k}_2 \cdot \vec{r}_2} = 2e^{i\vec{k} \cdot \vec{r}}$$

$$| | = 2$$

True all along mid plane.



$$|\vec{k}_1| \neq |\vec{k}_2|$$

$$e^{i\vec{k}_1 \cdot \vec{r}_1} + e^{i\vec{k}_2 \cdot \vec{r}_2} \neq 2 \cdot e^{i\vec{k}_1 \cdot \vec{r}_1}$$

destructive interference.

can even totally cancel!

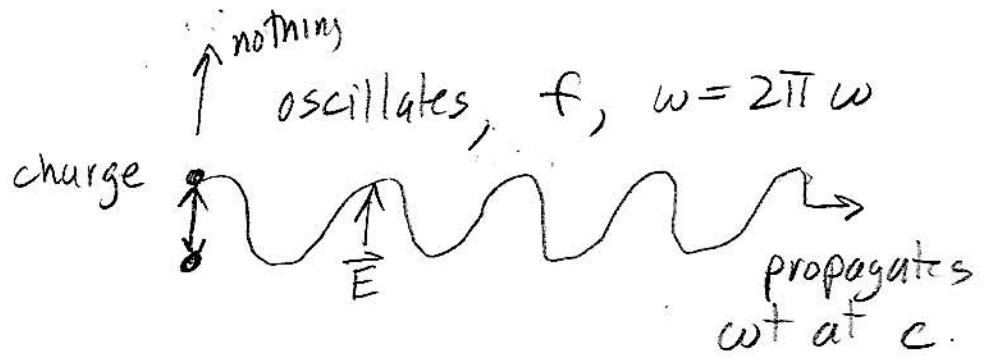
Key point  $|\vec{r}_2 - \vec{r}_1| < \text{coherence length}$   
for cancellation

Long Coherence Length = laser light

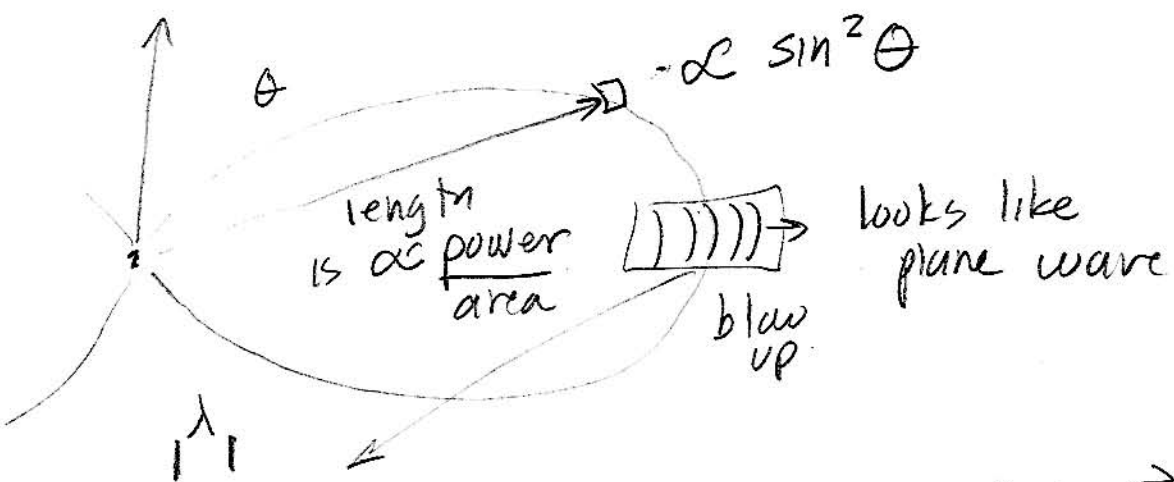
Short " " " = sunlight.

# Light Propagation

## Origin



Bigger scale:



$$e^{i(\omega t - \vec{k} \cdot \vec{r})}$$

$\omega \rightarrow$  given (by charge)

$$k = |\vec{k}| = \frac{2\pi}{\lambda}$$

speed  $\omega t - |\vec{k}| |\vec{r}| = 0$

(phase velocity) speed =  $\frac{|\vec{r}|}{t} = \frac{\omega}{|\vec{k}|} = \frac{2\pi \nu}{\frac{2\pi}{\lambda}}$

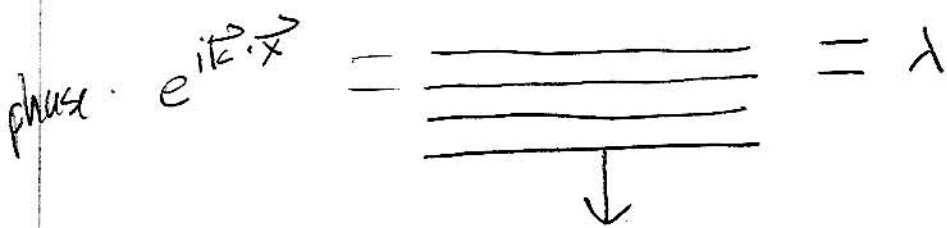
vacuum  $c = \lambda \nu$

When light goes into medium (water, glass, etc) light slows down... molecules radiate, absorb light; that takes time...

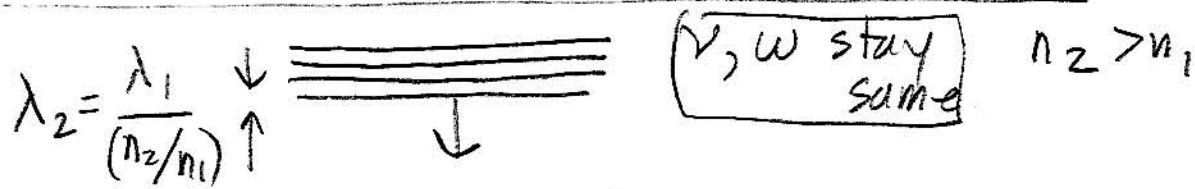
In medium:  $v \neq c$ ,  $v = \frac{c}{n} = \lambda \nu$

$n > 1$ , light slows down.

$n$ :	1.0002926	air	} visible
	1.333	water	
	2.419	diamond	
	10-100	infrared	



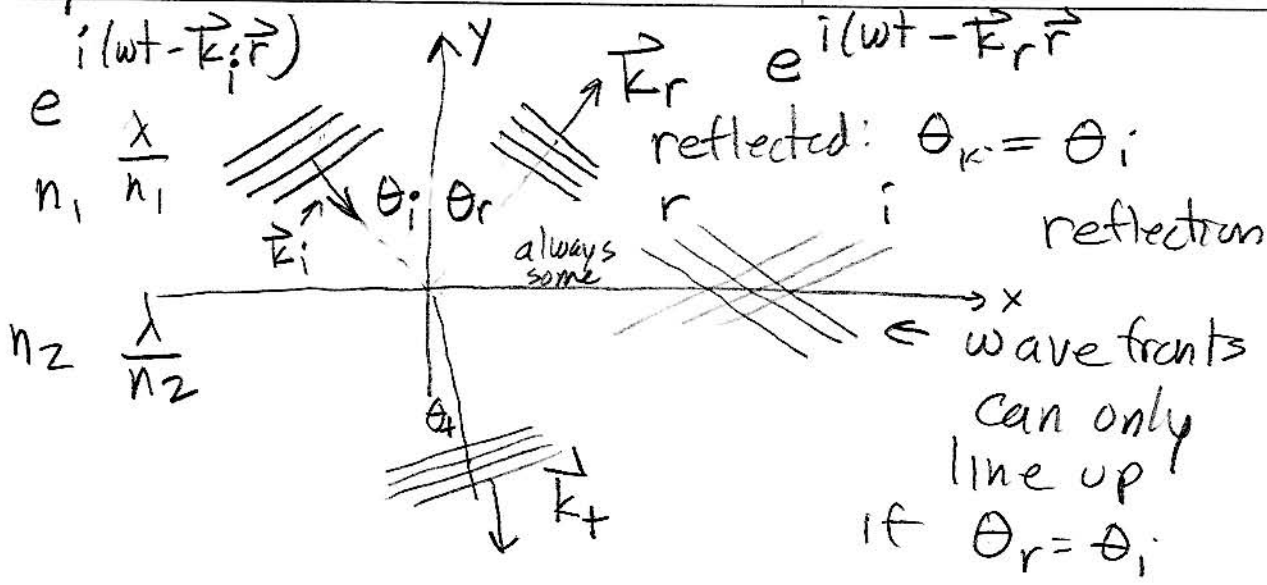
$n_1 \sim 1$



$\lambda_2 = \frac{\lambda_1}{(n_2/n_1)}$

$n_1 = 1, \lambda_2 = \frac{\lambda_1}{n}$  / consequences:

- ① radiation reflects at boundary.
- ② Refraction.



$$\vec{k}_i = \frac{n_1 \cdot 2\pi}{\lambda} (\sin \theta_i, -\cos \theta_i)$$

along  $y=0$  surface,

$$k_{ix} x = k_{rx} x$$

$$\frac{n_1 \cdot 2\pi}{\lambda} \sin \theta_i x = \frac{n_1 \cdot 2\pi}{\lambda} \sin \theta_r x$$

$$\sin \theta_i = \sin \theta_r$$

$$k_{ix} x = k_{tx} x$$

$$\frac{n_1 \cdot 2\pi}{\lambda} \sin \theta_i = \frac{n_2 \cdot 2\pi}{\lambda} \sin \theta_t$$

$$n_1 \sin \theta_i = n_2 \sin \theta_t$$

when  $n_2 > n_1$ ,  $\sin \theta_t < \sin \theta_i$