

$$F(b-R) + M a_x R = -\frac{I}{R} a_x$$

$$a_x \left(MR + \frac{I}{R} \right) = F(R-b)$$

$$a_x = \frac{R-b}{MR + \frac{I}{R}} F$$

$$a_x = \left(1 - \frac{b}{R} \right) \left(\frac{F}{M + \frac{I}{R^2}} \right)$$

> 0 , $I > 0$ reduces a_x

B: $I' a_x = -F(R-b) = -I' \frac{a_x}{R}$

$$I' = I + MR^2$$

$$F(R-b) = (I + MR^2) \frac{a_x}{R}$$

$$a_x = \frac{R(R-b)}{I + MR^2} F$$

$$a_x = \left(1 - \frac{b}{R} \right) \left(\frac{F}{M + \frac{I}{R^2}} \right)$$

Energy in Translational Motion

Translational : $\frac{1}{2} M v_{cm}^2$

Rotational : $\frac{1}{2} I_{cm} \omega^2$

No slipping : $\omega R = v_{cm}$

$$\frac{1}{2} M v_{cm}^2 + \frac{1}{2} I_{cm} \left(\frac{v_{cm}}{R} \right)^2$$

$$= \frac{1}{2} \left(M + \frac{I_{cm}}{R^2} \right) v_{cm}^2$$

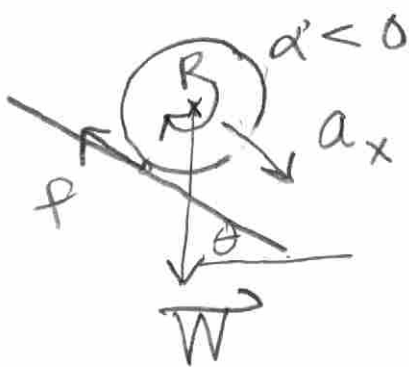


$$Mgh = \frac{1}{2} \left(M + \frac{I_{cm}}{R^2} \right) v_{cm}^2$$

$$v_{cm} = \left[\frac{2gh}{1 + \frac{I_{cm}}{MR^2}} \right]^{1/2}$$

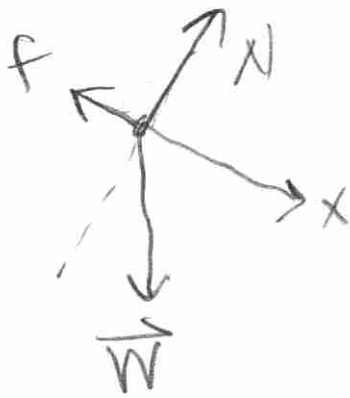
Demonstration

Does not address friction necessary to achieve rolling...



$$a_x = -\alpha R$$

$$\begin{aligned} \text{x component of } \vec{W} \\ = Mg \sin \theta \end{aligned}$$



$$\text{x: } Mg \sin \theta - f = M a_x$$

$$\text{y: } N - Mg \cos \theta = 0$$

$$N = Mg \cos \theta$$

$$f < \mu_s N = \mu_s Mg \cos \theta$$

Now solve for f

Use c.m. as rotation point.

$$I_{cm} \alpha = -fR = -I_{cm} \frac{a_x}{R}$$

$$\text{or } a_x = + \frac{fR^2}{I_{cm}}$$

$$Mg \sin \theta - f = \frac{MR^2}{I_{cm}} f$$

$$f = \frac{Mg \sin \theta}{1 + \frac{MR^2}{I_{cm}}} < \mu_s Mg \cos \theta$$

$$\tan \theta < \mu_s \left(1 + \frac{MR^2}{I_{cm}} \right)$$

rotation enables "steeper" incline, but remember, it rolls.

ball... $I_{cm} = \frac{2}{5} MR^2$

$$\tan \theta < \mu_s \left(1 + \frac{MR^2}{\frac{2}{5} MR^2} \right)$$

$$\tan \theta < \frac{7}{2} \mu_s$$